Chapter 11

Multiply Fractions and Whole Numbers



► Relate Addition to Multiplication Complete.

2. + ___ + ___ = ___

× =

► Read and Write Mixed Numbers Write a mixed number for the shaded part. Write a fraction for the unshaded part.

3.

Shaded: _____

Unshaded:

4.

Shaded: _____

Unshaded: _____

▶ Part of a Group Write a fraction that names the shaded part.

1.

shaded parts _____total parts ____

fraction

shaded parts _____ total parts _____

fraction _____

MATH in the World

The budget for Carter Museum's annual party is \$10,000. Food accounts for $\frac{1}{2}$ of the budget, beverages for $\frac{1}{4}$, and decorations for $\frac{1}{10}$ of the budget. The remainder is spent on staffing the party. How much money is spent on staffing the party?

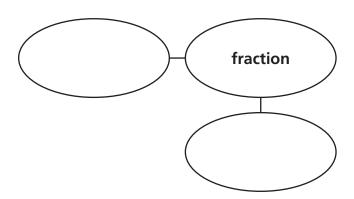


Vocabulary Builder

Go Online For more help

Visualize It

Complete the bubble map using the review words.



Connect to Vocabulary

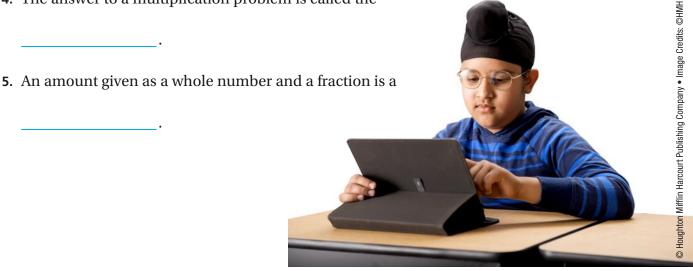
Review Words

fraction mixed number multiple product unit fraction

▶ Understand Vocabulary

Complete the sentences.

- 1. A _____ can name a part of a group or a whole.
- **2**. You can write ______ of 10 such as 10, 20, 30, and so on.
- 3. _____ have one as the numerator.
- **4.** The answer to a multiplication problem is called the



Lesson 1

Multiples of Unit Fractions

(I Can) find multiples of a unit fraction by multiplying a unit fraction by a whole number.

- Algebraic Reasoning 4.AR.1.3
- Fractions 4.FR.2.4
- Mathematical Thinking & Reasoning MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1

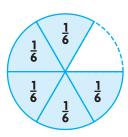


UNLOCK the Problem



At a pizza party, each pizza was cut into 6 equal slices. At the end of the party, there was $\frac{5}{6}$ of a pizza left. Roberta put each of the leftover slices in its own freezer bag. How many bags did she use? What part of a pizza did she put in each bag?

Example Write $\frac{5}{6}$ as the product of a whole number and a unit fraction.



The picture shows $\frac{5}{6}$ or

sixth-size pieces.

Each sixth-size pieces of the pizza can be shown by the

unit fraction .

You can use unit fractions to show $\frac{5}{6}$ in two ways.

$$\frac{5}{6}$$
 = _____ + ____ + ____ + ____ + ____ + ____

$$\frac{5}{6} = \underline{\qquad} \times \frac{1}{6}$$

 How many slices of pizza were eaten?

What fraction of the pizza is 1 slice?

Remember

You can use multiplication to show repeated addition.

$$3 \times 4$$
 means $4 + 4 + 4$.

$$4 \times 2$$
 means $2 + 2 + 2 + 2$.



MTR Complete tasks with 3.1 mathematical fluency.

Give an example of how you would write a fraction greater than 1 as a mixed number.

The number of addends, or the multiplier, represents the number of bags used.

The unit fractions represent the part of a pizza in each bag.

So, Roberta used _____ bags. She put ____ of a pizza in each bag.

• Explain how you can write $\frac{3}{2}$ as the product of a whole number and a unit fraction.

Multiples The product of a number and a counting number is a multiple of the number. You have learned about multiples of whole numbers.

The products 1 \times 4, 2 \times 4, 3 \times 4, and so on are multiples of 4.

The numbers 4, 8, 12, and so on are multiples of 4.

You can also find multiples of unit fractions.

$1 \times \frac{1}{4}$ is $\frac{1}{4}$. Use models to write the next four multiples of $\frac{1}{4}$. Complete the last model.

1/4	<u>1</u>	<u>1</u>	<u>1</u>	$2 \times \frac{1}{4}$
1/4	1/4	1/4	1/4	$=\frac{2}{4}$

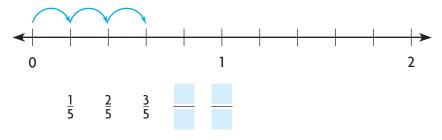
1/4	<u>1</u>	<u>1</u>	<u>1</u>	3×
1/4	<u>1</u>	1/4	<u>1</u>	
1/4	<u>1</u>	<u>1</u>	<u>1</u>	= 4

1/4	1/4	1/4	1/4	
1/4	1/4	1/4	1/4	4 × —
1/4	1/4	1/4	1/4	= 4
1/4	<u>1</u>	<u>1</u>	1/4	

1/4	<u>1</u>	<u>1</u>	<u>1</u>	
1/4	1/4	1/4	1/4	
1/4	1/4	1/4	1/4	
1/4	1/4	1/4	1/4	=
1/4	1/4	1/4	1/4	

Multiples of $\frac{1}{4}$ are $\frac{1}{4}$, , , and

Use a number line to write multiples of $\frac{1}{5}$.



Multiples of $\frac{1}{5}$ are $\frac{1}{5}$, , , and

Share and Show

1. Use the picture to complete the equations.

	1	l	
<u>1</u>	<u>1</u>	<u>1</u>	

$$\frac{3}{4} = \underline{\qquad} \times \frac{1}{4}$$

Write the fraction as a product of a whole number and a unit fraction.

2.
$$\frac{4}{5} =$$

4.
$$\frac{8}{3} =$$

List the next four multiples of the unit fraction.

5.
$$\frac{1}{6}$$
,











Explain why $\frac{8}{5}$ is a multiple

On Your Own

Write the fraction as a product of a whole number and a unit fraction.

7.
$$\frac{5}{6} =$$

8.
$$\frac{9}{4} =$$

9.
$$\frac{3}{100} =$$

List the next four multiples of the unit fraction.

10.
$$\frac{1}{10}$$



11.
$$\frac{1}{8}$$
,



Problem Solving · Applications World



- **12.** MTR Ailee uses $\frac{1}{2}$ cup of blueberries to make each loaf of blueberry bread. Explain how many loaves of blueberry bread she can make with $2\frac{1}{2}$ cups of blueberries.
- 13. Sinna cut a loaf of bread into 12 equal slices. His family ate some of the bread and now $\frac{5}{12}$ of the loaf is left. Sinna wants to put each of the leftover slices in its own bag. How many bags does Sinna need?
- **14.** Which fraction is a multiple of $\frac{1}{5}$? Mark all that apply.
- $\circ \frac{5}{16} \circ \frac{3}{5}$

15. Whose statement makes sense? Whose statement is nonsense? Explain your reasoning.



There is no multiple of $\frac{1}{6}$ between $\frac{3}{6}$ and $\frac{4}{6}$.



 $\frac{4}{5}$ is a multiple of $\frac{1}{4}$.

Gavin

Meera				

For the statement that is nonsense, write a new statement that makes sense.

Multiples of Unit Fractions

Go Online Interactive Examples

Write the fraction as a product of a whole number and a unit fraction.

1.
$$\frac{5}{6} = \underline{\qquad \qquad 5 \times \frac{1}{6} \qquad \qquad }$$
 2. $\frac{7}{8} = \underline{\qquad \qquad }$

2.
$$\frac{7}{8} =$$

3.
$$\frac{5}{3} =$$

4.
$$\frac{9}{10} =$$
 _____ **5.** $\frac{3}{4} =$ _____ **6.** $\frac{11}{12} =$ _____

5.
$$\frac{3}{4}$$
 =

6.
$$\frac{11}{12} =$$

List the next four multiples of the unit fraction.

7.
$$\frac{1}{5}$$
, ______, ______

Problem Solving Real World

- **9.** So far, Midori has read $\frac{5}{6}$ of a book. She has **10.** Nicholas buys $\frac{3}{8}$ pound of cheese. He read the same number of pages each day for 5 days. What fraction of the book does Midori read each day?
 - puts the same amount of cheese on 3 sandwiches. How much cheese does Nicholas put on each sandwich?
- **11.** Explain how to write $\frac{5}{3}$ as a product of a whole number and a unit fraction.

Lesson Check

- **12.** Selena walks from home to school each morning and back home each afternoon. Altogether, she walks $\frac{2}{3}$ mile each day. How far does Selena live from school?
- **13.** Will uses $\frac{3}{4}$ cup of olive oil to make 3 batches of salad dressing. How much oil does Will use for one batch of salad dressing?

Spiral Review

- **14.** Liza bought $\frac{5}{8}$ pound of trail mix. She gives $\frac{2}{8}$ pound of trail mix to Michael. How much trail mix does Liza have left?
- **15.** Ximena has a piece of rope that is $6\frac{2}{3}$ feet long. How do you write $6\frac{2}{3}$ as a fraction greater than 1?

16. A group of students makes a pattern with their house numbers. Kyrie's house number is missing. What is Kyries house number?

29, 39, ?, 59, 69, 79

17. Blima buys 12 cupcakes. Nine of the cupcakes have chocolate frosting and the rest have vanilla frosting. What fraction of the cupcakes have vanilla frosting?

Multiples of Fractions

I Can find multiples of fractions by multiplying a fraction by a whole number.



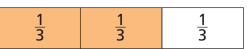
- Algebraic Reasoning 4.AR.1.3
- Fractions 4.FR.2.4
- Mathematical Thinking & Reasoning MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1



UNLOCK the Problem Real World

Gema is making 4 pans of baked ziti. For each pan, she needs $\frac{2}{3}$ cup cheese. Her measuring cup can scoop $\frac{1}{3}$ cup of cheese. How many scoops of cheese does she need for the 4 pans?

Example 1 Use a model to write the product $4 \times \frac{2}{3}$ as the product of a whole number and a unit fraction.



Think: $\frac{2}{3}$ is 2 third-size pieces.

$$\frac{2}{3} =$$
_____ + ____ or 2 × ____

There are 4 pans of baked ziti. Each pan needs $\frac{2}{3}$ cup cheese.



$$\leftarrow$$
 1 pan: 2 $\times \frac{1}{3} = \frac{2}{3}$

$$\frac{1}{3}$$
 $\frac{1}{3}$ $\frac{1}{3}$

$$\leftarrow$$
 2 pans: $2 \times 2 \times \frac{1}{3} = 4 \times \frac{1}{3} = \frac{4}{3}$

$$\frac{1}{3}$$
 $\frac{1}{3}$ $\frac{1}{3}$

$$\leftarrow$$
 3 pans: $3 \times 2 \times \frac{1}{3} = 6 \times \frac{1}{3} = \frac{6}{3}$

$$\frac{1}{3}$$
 $\frac{1}{3}$ $\frac{1}{3}$

← 4 pans:
$$4 \times 2 \times \frac{1}{3} = 8 \times \frac{1}{3} = \frac{8}{3}$$

$$4 \times \frac{2}{3} = 4 \times \underline{\hspace{1cm}} \times \frac{1}{3} = \underline{\hspace{1cm}} \times \frac{1}{3} = \underline{\hspace{1cm}}$$



So, Gema needs _____ third-size scoops of cheese for 4 pans of ziti.

3.1 mathematical fluency. Explain how this model of $4 \times \frac{2}{3}$ is related to a model of 4×2 .

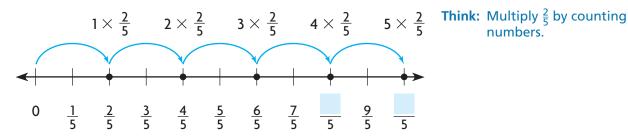
MTR Complete tasks with

1. What if Gema decides to make 10 pans of ziti? Describe a pattern you could use to find the number of scoops of cheese she would need.

Multiples You have learned to write multiples of unit fractions.

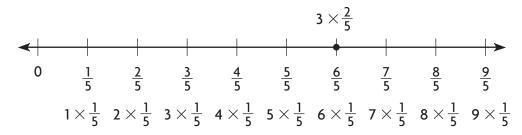
You can also write multiples of non-unit fractions.

Example 2 Use a number line to write multiples of $\frac{2}{5}$.



Multiples of $\frac{2}{5}$ are $\frac{2}{5}$, , , and .

 $3 \times \frac{2}{5} = \frac{6}{5}$. Write $\frac{6}{5}$ as a product of a whole number and a unit fraction.



$$3 \times \frac{2}{5} = \frac{6}{5} =$$
_____ \times _____

2. Explain how to use repeated addition to write the multiple of a fraction as the product of a whole number and a unit fraction.

Share and Show

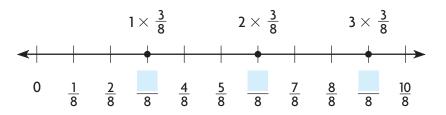
Math

1. Write three multiples of $\frac{3}{8}$.

$$1 \times \frac{3}{8} = \underline{\hspace{1cm}}$$

 $2 \times \frac{3}{8} =$ _____

 $3 \times \frac{3}{9} =$



Multiples of $\frac{3}{8}$ are _____, and _____.



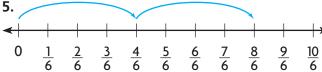




Write the product as the product of a whole number and a unit fraction.



$$3 \times \frac{3}{4} =$$



$$2 \times \frac{4}{6} =$$



MTR Engage in discussions on 4.1 mathematical thinking.

Explain how to write a product of a whole number and a fraction as a product of a whole number and a unit fraction.

On Your Own

List the next four multiples of the fraction.

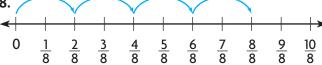








Write the product as the product of a whole number and a unit fraction.



$$4 \times \frac{2}{8} =$$



$$3 \times \frac{3}{5} = \underline{\hspace{1cm}}$$

- **10.** Are $\frac{6}{10}$ and $\frac{6}{30}$ multiples of $\frac{3}{10}$? Explain.
- **11.** Which is greater, $4 \times \frac{2}{16}$ or $3 \times \frac{3}{16}$? Explain.

Problem Solving · Applications World



12. Shulem is watering his plants. He gives each of 2 plants $\frac{3}{5}$ pint of water. His watering can holds $\frac{1}{5}$ pint. How many times will he fill his watering can to water both plants?





What do you need to find?

b. What information do you need to use?				

How can drawing a model help you solve the problem?

Show the steps you use to solve the problem.

e. Complete the sentence. Shulem will fill his watering can _____times.

13. Alma is making 3 batches of tortillas. She adds $\frac{3}{4}$ cup of water to each batch. The measuring cup holds $\frac{1}{4}$ cup. How many times must Alma measure $\frac{1}{4}$ cup of water to have enough for the tortillas? Shade the model to show your answer.

Alma must measure $\frac{1}{4}$ cup times.

1/4	<u>1</u>	<u>1</u>	<u>1</u>
1/4	<u>1</u>	<u>1</u>	1/4
1/4	1/4	1/4	1/4

Multiples of Fractions

Go Online
Interactive Examples

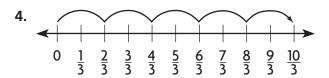
List the next four multiples of the fraction.

1.
$$\frac{3}{5}$$
,,

2.
$$\frac{2}{6}$$

Write the product as the product of a whole number and a unit fraction.

3.



$$2 \times \frac{4}{5} = \underline{\hspace{1cm}}$$

$$5 \times \frac{2}{3} = \underline{\hspace{1cm}}$$

Problem Solving Real World

- 5. Lia is making 2 loaves of banana bread. She needs $\frac{3}{4}$ cup of sugar for each loaf. Her measuring cup can only hold $\frac{1}{4}$ cup of sugar. How many times will Lia need to fill the measuring cup in order to get enough sugar for both loaves of bread?
- **6.** A group of 4 students is performing an experiment with salt. Each student must add $\frac{3}{8}$ teaspoon of salt to a solution. The group only has a $\frac{1}{8}$ -teaspoon measuring spoon. How many times will the group need to fill the measuring spoon in order to perform the experiment?
- 7. Explain how to write $3 \times \frac{3}{8}$ as the product of a whole number and a unit fraction.

Lesson Check

- **8.** Eloise made a list of some multiples of $\frac{8}{5}$. Write 5 fractions that could be in Eloise's list.
- **9.** David is filling five $\frac{3}{4}$ -quart bottles with a sports drink. His measuring cup only holds $\frac{1}{4}$ quart. How many times will David need to fill the measuring cup in order to fill the 5 bottles?

Spiral Review

- **10.** Ira has 128 stamps in his stamp album. He has the same number of stamps on each of the 8 pages. How many stamps are on each page?
- **11.** Enrique is saving up for a bike that costs \$198. So far, he has saved \$15 per week for the last 12 weeks. How much more money does Enrique need in order to be able to buy the bike?

- **12.** Amalia buys $3\frac{7}{8}$ yards of material at the fabric store. She uses it to make a skirt. Afterward, she has $1\frac{3}{8}$ yards of the fabric left over. How many yards of material did Amalia use?
- 13. Order these fractions from least to **greatest:** $\frac{2}{3}$, $\frac{7}{12}$, $\frac{3}{4}$

Name

Multiply a Fraction by a Whole Number Using Models

I Can use a model to multiply a fraction by a whole number.

- Algebraic Reasoning 4.AR.1.3
- Fractions 4.FR.2.4
- Mathematical Thinking & Reasoning MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1

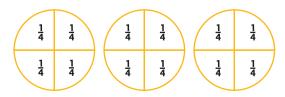


UNLOCK the Problem Real World

Khai practices the violin for $\frac{3}{4}$ hour each day. He has a recital in 3 days. How much time will he practice in 3 days?

Example 1 Use a model to multiply $3 \times \frac{3}{4}$.

Think: $3 \times \frac{3}{4}$ is 3 groups of $\frac{3}{4}$ of a whole. Shade the model to show 3 groups of $\frac{3}{4}$.



1 group of
$$\frac{3}{4} = _____$$

2 groups of
$$\frac{3}{4}$$
 =

3 groups of
$$\frac{3}{4}$$
 =

$$3 \times \frac{3}{4} =$$

So, Khai will practice for _____ hours in all.

• How many equal groups of $\frac{3}{4}$ should you model?





MTR Complete tasks with mathematical fluency.

If you multiply $4 \times \frac{2}{6}$, is the product greater than or less than 4? Explain.

- **1.** Explain how you can use repeated addition with the model to find the product $3 \times \frac{3}{4}$.
- **2.** Khai's daily practice of $\frac{3}{4}$ hour is in sessions that last for $\frac{1}{4}$ hour each. Describe how the model shows the number of practice sessions Khai has in 3 days.

Example 2 Use a pattern to multiply.

You know how to use a model and repeated addition to multiply a fraction by a whole number. Look for a pattern in the table to discover another way to multiply a fraction by a whole number.

Multiplication problem		Whole number (number of groups)	Fraction (size of groups)	Product
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$2 \times \frac{1}{6}$	2	$\frac{1}{6}$ of a whole	<u>2</u> 6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$2 imes \frac{2}{6}$	2	$\frac{2}{6}$ of a whole	<u>4</u> 6
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$2 \times \frac{3}{6}$	2	$\frac{3}{6}$ of a whole	<u>6</u>

When you multiply a fraction by a whole number, the numerator

in the product is the product of the _____ and the

of the fraction. The denominator in the product

is the same as the ______ of the fraction.

- 3. How do you multiply a fraction by a whole number without using a model or repeated addition?
- **4.** Describe two different ways to find the product $4 \times \frac{2}{3}$.

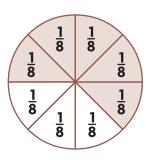
Share and Show

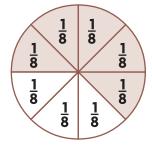


1. Find the product $3 \times \frac{5}{8}$.

$$3 \times \frac{5}{8} =$$

1/8	18	18	18
18	18	18	18

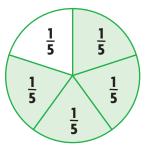


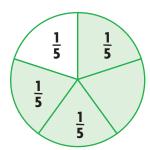


3 groups of
$$\frac{5}{8}$$

Multiply.







3.

<u>1</u>	1 3	<u>1</u>
<u>1</u> 3	1/3	1/3
1/3	1/3	1/3
1/3	1/3	1/3

$$4 \times \frac{2}{3} =$$

 $2 \times \frac{4}{5} = \underline{\hspace{1cm}}$

 \checkmark 4. $5 \times \frac{3}{10} =$

5. $4 \times \frac{5}{6} =$

Math Talk

MTR Complete tasks with mathematical fluency.

Describe how to model Problem 5.

On Your Own

Multiply.

6.
$$2 \times \frac{7}{12} =$$

7.
$$6 \times \frac{3}{8} =$$

8.
$$5 \times \frac{2}{4} =$$

9.
$$3 \times \frac{4}{6} =$$

10.
$$2 \times \frac{5}{10} =$$

11.
$$4 \times \frac{2}{8} =$$

MTR Write the unknown number.

12.
$$\times \frac{2}{3} = \frac{12}{3}$$

14.
$$2 \times \frac{7}{8} = \frac{14}{8}$$

Problem Solving · Applications World



15. Eloisa makes clothes for pets. She needs $\frac{5}{6}$ yard of fabric to make 1 dog coat. How much fabric does she need to make 3 dog coats?





- a. What do you need to find?
- b. What information do you need?
- **c.** Show the steps you use to solve the problem.

d. Complete the sentence.

Eloisa needs _____ yards of fabric to make 3 dog coats.

- **16.** Manuel's small dog eats $\frac{2}{4}$ bag of dog food in 1 month. His large dog eats $\frac{3}{4}$ bag of dog food in 1 month. How many bags do both dogs eat in 6 months?
- **17.** Select the correct product for the equation.

24	
12	

$$9 \times \frac{2}{12} =$$

$$3 \times \frac{6}{16} =$$

$$6 \times \frac{4}{16} =$$

$$8 \times \frac{3}{12} =$$

Multiply a Fraction by a Whole Number Using Models

Go Online

Interactive Examples

Multiply.

1.
$$2 \times \frac{5}{6} = \frac{10}{6}$$

2.
$$3 \times \frac{2}{5} =$$

3.
$$7 \times \frac{3}{10} =$$

4.
$$3 \times \frac{5}{12} =$$
 _____ **5.** $6 \times \frac{3}{4} =$ _____

5.
$$6 \times \frac{3}{4} =$$

6.
$$4 \times \frac{2}{5} =$$

Problem Solving Real World

- **7.** Ivan walks $\frac{5}{8}$ mile to the bus stop each morning. How far will he walk in 5 days?
- **8.** Milana uses $\frac{2}{3}$ cup of milk to make one batch of muffins. How many cups of milk will Milana use if she makes 3 batches of muffins?

9. Explain how you can use a model to find $4 \times \frac{3}{8}$. Include a drawing and a solution.

Lesson Check

- **10.** Aleta's puppy gained $\frac{3}{8}$ pound each week for 4 weeks. Altogether, how much weight did the puppy gain during the 4 weeks?
- **11.** Pedro mixes $\frac{3}{4}$ teaspoon of plant food into each gallon of water. How many teaspoons of plant food should Pedro mix into 5 gallons of water?

Spiral Review

- 12. Ivana has $\frac{3}{4}$ pound of hamburger meat. She makes 3 hamburger patties. Each patty weighs the same amount. How much does each hamburger patty weigh?
- **13.** Write $\frac{7}{10}$ as a sum of fractions two different ways.

- **14.** Arjun wants to find the total length of 3 boards. He uses the expression $3\frac{1}{2}+(2+4\frac{1}{2})$. How can Arjun rewrite the expression using both the Associative and Commutative Properties of Addition?
- **15.** Fill in the blank with a symbol that makes this statement true:

$$\frac{5}{12}$$
 $\frac{1}{3}$

Lesson 4

Find Part of a Group

(I Can) find part of a group by multiplying a whole number by a fraction.

Florida's B.E.S.T.

- Algebraic Reasoning 4.AR.1.3
- Fractions 4.FR.2.4
- Mathematical Thinking & Reasoning MTR.1.1, MTR.3.1, MTR.4.1, MTR.5.1,



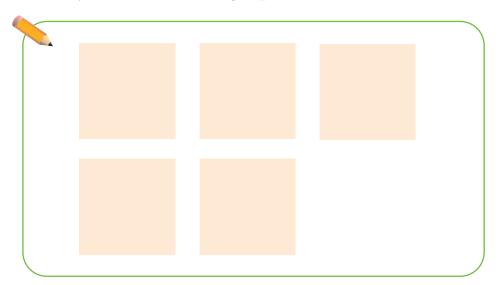
🗄 UNLOCK the Problem Real World

Maya collects stamps. She has 20 stamps in her collection. Four-fifths of her stamps have been canceled. How many of the stamps in Maya's collection have been canceled? Find $\frac{4}{5}$ of 20.

- Put 20 counters on your MathBoard. Since you want to find $\frac{4}{5}$ of the stamps, you should arrange the 20 counters in equal groups.
- Draw the counters in equal groups below. How many counters are in each group?



▲ The post office cancels stamps to keep them from being reused.



Each group represents _____ of the stamps. Circle $\frac{4}{5}$ of the counters.

How many groups did you circle? _____

How many counters did you circle?_____

$$\frac{4}{5}$$
 of 20 = ____, or $\frac{4}{5} \times 20 = _____$

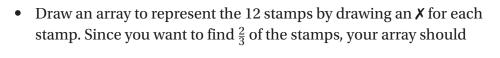
So, _____ of the stamps have been canceled.

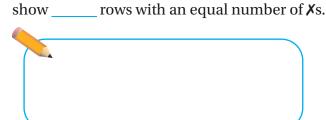
MTR Complete tasks with 3.1 mathematical fluency.

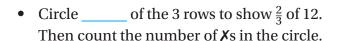
How many groups would you circle if $\frac{3}{5}$ of the stamps were canceled? Explain.

Example

Alejandro's stamp collection has stamps from different countries. He has 12 stamps from Canada. Of those twelve, $\frac{2}{3}$ of them have pictures of Queen Elizabeth II. How many stamps have the queen on them?







There are Xs circled.

• Complete the equations.

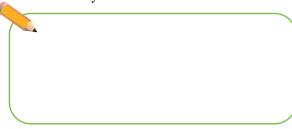
$$\frac{2}{3}$$
 of $12 =$ _____, or $\frac{2}{3} \times 12 =$ _____

So, there are _____ stamps with a picture of Queen Elizabeth II.

• MTR On your MathBoard, use counters to find $\frac{4}{6}$ of 12. Explain why the answer is the same as the answer when you found $\frac{2}{3}$ of 12.

Try This! Draw an array.

Zainab has 16 stamps. In her collection, $\frac{3}{4}$ of the stamps are from the United States. How many of her stamps are from the United States and how many are not?



So, _____ of Zainab's stamps are from the United States, and _____ stamps are not.



1. Complete the model to solve.

$$\frac{7}{8}$$
 of 16, or $\frac{7}{8} \times 16$

- How many rows of counters are there?
- How many counters are in each row?
- Circle _____ rows to solve the problem.
- How many counters are circled?

$$\frac{7}{8}$$
 of $16 =$ _____, or $\frac{7}{8} \times 16 =$ _____



Use a model to solve.

2.
$$\frac{2}{3} \times 18 =$$

2.
$$\frac{2}{3} \times 18 =$$
 3. $\frac{2}{5} \times 15 =$

⊘ 4.
$$\frac{2}{3}$$
 × 6 = _____



MTR Complete tasks with 3.1 mathematical fluency.

Explain how you used a model to solve Problem 4.

On Your Own

Use a model to solve.

5.
$$\frac{5}{8} \times 24 =$$

6.
$$\frac{3}{4} \times 24 =$$

7.
$$\frac{4}{3} \times 21 =$$

Solve.

8. MTR What multiplication problem does the model represent?



Problem Solving · Applications

Use the table for Problems 9 and 10.

- 9. MTR Four-fifths of Zack's stamps have pictures of animals. How many stamps with pictures of animals does Zack have? Use a model to solve.
- **10.** Zack, Teri, and Paco combined the foreign stamps from their collections for a stamp show. Out of their collections, $\frac{3}{10}$ of Zack's stamps, $\frac{5}{6}$ of Teri's stamps, and $\frac{3}{8}$ of Paco's stamps were from foreign countries. How many stamps were in their display? Explain how you solved the problem.

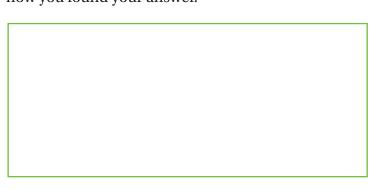
Stamps Collected						
Name	Number of stamps					
Zack	30					
Teri	18					
Paco	24					



	_		_		_
C	h	-	the	N/1-	.+ h
3	П	UVV	une	IVIC	1 L I I

Demonstrate Your Thinking

- **11.** Hwasa has 24 stamps in her collection. Among her stamps, $\frac{1}{3}$ have pictures of animals. Out of her stamps with pictures of animals, $\frac{3}{4}$ of those stamps have pictures of birds. How many stamps have pictures of birds on them?
- **12.** Onda bought 16 songs for her MP3 player. Three-fourths of the songs are classical songs. How many of the songs are classical songs? Draw a model to show how you found your answer.



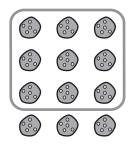
Find Part of a Group

Go Online

Interactive Examples

Use a model to solve.

1.
$$\frac{3}{4} \times 12 = 9$$



2.
$$\frac{7}{8} \times 16 =$$

3.
$$\frac{6}{10} \times 10 =$$

4.
$$\frac{2}{3} \times 9 =$$

5.
$$\frac{1}{6} \times 18 =$$

6.
$$\frac{4}{5} \times 10 =$$

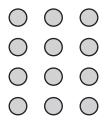
Problem Solving Real World

- 7. Marco drew 20 pictures. He drew $\frac{3}{4}$ of them in art class. How many pictures did Marco draw in art class?
- **8.** Carolina has 10 marbles. One half of them are blue. How many of Carolina's marbles are blue?

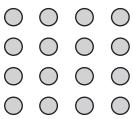
9. Explain how to find $\frac{3}{4}$ of 20 using a model. Include a drawing.

Lesson Check

10. Use the model to find $\frac{1}{3} \times 15$.



11. Use the model to find $\frac{2}{4} \times 16$.



Spiral Review

12. What is the value of the underlined digit?

13. Nigel has 138 fluid ounces of lemonade. How many 6-fluid-ounce servings of lemonade can he make?

6,560

- **14.** Rafi had a board that was $15\frac{5}{8}$ feet long. He cut off a piece of the board that is $11\frac{3}{8}$ feet long. How much of the board is left?
- **15.** Silvia spent $4\frac{2}{8}$ hours during one week and $3\frac{5}{8}$ hours during another week working on a history project. About how long did she spend working on the project?

Name

Multiply Fractions and Whole Numbers

I Can use models to multiply fractions by whole numbers or whole number by fractions.

Florida's B.E.S.T.

- Algebraic Reasoning 4.AR.1.3
- Fractions 4.FR.2.4
- Mathematical Thinking & Reasoning MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1

Investigate

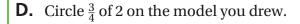
Martin is planting a vegetable garden. Each row is 2 meters long. He wants to plant carrots along $\frac{3}{4}$ of each row. How many meters of each row will he plant with carrots?

Multiply. $\frac{3}{4} \times 2$

Materials ■ fraction strips ■ MathBoard

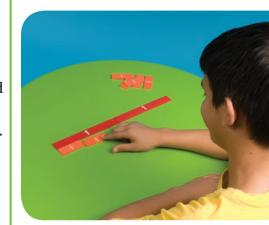
- **A.** Place two 1-whole fraction strips side-by-side to represent the length of each row.
- **B.** To represent the denominator of the factor $\frac{3}{4}$, the 2 wholes need to be separated into 4 equal parts. So, find 4 fraction strips, all with the same denominator, that fit exactly under the two wholes.
- **C.** Draw a picture of your model.





E. Complete the number sentence. $\frac{3}{4} \times 2 =$

So, Martin will plant carrots along _____ meters of each row.



Draw Conclusions

- **1. MTR** Explain why you placed four fraction strips with the same denominator under the two 1-whole strips.
- **2. MTR** Explain how you would model $\frac{3}{10}$ of 2.

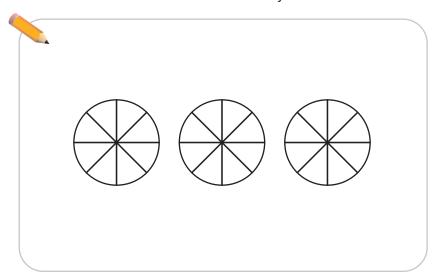
Make Connections

In the Investigate activity, you multiplied a whole number by a fraction. You can also use a model to multiply a fraction by a whole number.

Thuy was helping clean up after a class party. There were 3 boxes remaining with pizza in them. Each box had $\frac{3}{8}$ of a pizza left. How much pizza was left in all?

Materials fraction circles

- **STEP 1** Find $3 \times \frac{3}{8}$. Model three 1-whole fraction circles to represent the number of boxes containing pizza.
- **STEP 2** Place $\frac{1}{8}$ fraction circle pieces on each circle to represent the amount of pizza that was left in each box.
 - Shade the fraction circles below to show your model.





The 3 circles show _____ eighths.

STEP 3 Complete the number sentences.

$$\frac{3}{8} + \frac{3}{8} + \frac{3}{8} =$$

$$3 \times \frac{3}{8} =$$

So, Thuy had _____ pizzas left.



MTR Engage in discussions on 4.1 mathematical thinking.

Explain how you would know there is more than one pizza left.

Share and Show

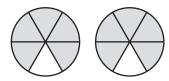


Use the model to find the product.

1.
$$\frac{5}{6} \times 3 =$$

1		1		1		
1/2	1/2	1/2	1/2	1/2	1/2	

2.
$$2 \times \frac{5}{6} =$$



Find the product.

3.
$$\frac{5}{12} \times 3 =$$

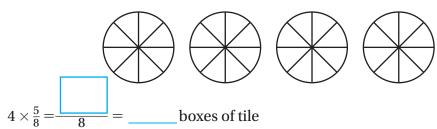
3.
$$\frac{5}{12} \times 3 =$$
 4. $9 \times \frac{1}{3} =$

⊙ 5.
$$\frac{7}{8} \times 4 =$$

Problem Solving • Applications

6. Naela brought 3 pans of homemade fruit bars to school. Her classmates at $\frac{7}{12}$ of each pan. Naela gave 1 whole pan of the leftover fruit bars to the school's secretaries and took the rest home. Explain how to find how much of a pan of fruit bars Naela took home.

7. Huyen is cleaning up after tiling a bathroom. There are 4 open boxes of tile. Each box has $\frac{5}{8}$ of the tiles remaining. How many boxes of tile are left? Shade the model and complete the calculations below to show how you found your answer.



Pose problems.		Solve your	oroblems.
How could you change the model to give y Explain and write a new equation.	ou an answer	of $4\frac{4}{5}$?	MATH on the > Spot

Multiply Fractions and Whole Numbers

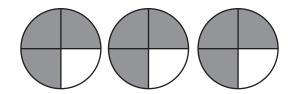
Go Online Interactive Examples

Use the model to find the product.

1.
$$\frac{5}{12} \times 3 = \frac{5}{4}$$
, or $1\frac{1}{4}$

1		1			1						
1/4	<u>1</u>	<u>1</u>	<u>1</u>	1/4	<u>1</u>						

2.
$$3 \times \frac{3}{4} =$$



Find the product.

4.
$$7 \times \frac{2}{3} =$$

5.
$$\frac{3}{8} \times 4 =$$

6.
$$7 \times \frac{5}{6} =$$

7.
$$\frac{5}{12} \times 6 =$$

8.
$$9 \times \frac{2}{3} =$$

Problem Solving Real World

- uses $\frac{4}{5}$ of the bag to make potato salad. How many pounds of potatoes does Jody use for the potato salad?
- **9.** Jody has a 5-pound bag of potatoes. She **10.** Lucas lives $\frac{5}{8}$ mile from school. Kenny lives twice as far as Lucas from school. How many miles does Kenny live from school?

11. Explain how to use models to find $3 \times \frac{3}{4}$ and $\frac{3}{4} \times 3$. Include a picture of each model.

Lesson Check

- **12.** In gym class, Ted runs $\frac{4}{5}$ mile. His teacher runs 6 times that distance each day. How many miles does Ted's teacher run each day?
- **13.** Zico is decorating a banner for a parade. Zico uses a piece of red ribbon, which is $\frac{3}{4}$ yard long. Zico also needs blue ribbon that is 5 times as long as the red ribbon. How much blue ribbon does Zico need?

Spiral Review

- 14. Mirror Lake Elementary School has 168 students and chaperones going on the fifth-grade class trip. Each bus can hold 54 people. What is the least number of buses needed for the trip?
- **15.** A carpenter has a board $3\frac{1}{4}$ feet long. She sawed off a piece that is $2\frac{3}{4}$ feet long. How much of the board was left?

16. Write $7\frac{9}{12}$ as a fraction.

17. What is an equivalent fraction for $\frac{76}{100}$?

Lesson 6

Fraction and Whole-Number Multiplication

(I Can) solve real-world problems that multiply a fraction by a whole number or a whole number by a fraction.

Florida's B.E.S.T.

- Algebraic Reasoning 4.AR.1.3
- Mathematical Thinking & Reasoning MTR.3.1, MTR.4.1, MTR.5.1, MTR.6.1

UNLOCK the Problem



Charlene has five 1-pound bags of sand, each a pound of each bag of sand to create a colorful sand-art jar. How much sand will be in Charlene's sand-art jar?

different color. For an art project, she will use $\frac{3}{8}$

• How much sand is in each bag?

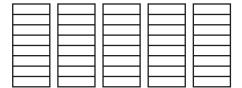
• Will Charlene use all of the sand in each bag? Explain.

Multiply a fraction by a whole number.

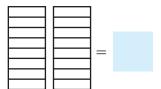
MODEL

Shade the model to show 5 groups of ³/₈.





 Rearrange the shaded pieces to fill as many wholes as possible.

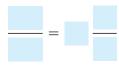


- **RECORD**
- Write an expression to represent the problem.

Think: I need to find 5 groups of 3 eighth-size

• Multiply the number of eighth-size pieces in each whole by 5. Then write the answer as the total number of eighth-size pieces.

Write the answer as a mixed number.



So, there are _____ pounds of sand in Charlene's sand-art jar.



MTR Engage in discussions on mathematical thinking.

Explain how you can find how much sand Charlene has left.

Example Multiply a whole number by a fraction.

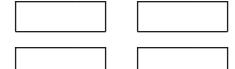
Inaaya brought in 4 loaves of sliced bread to make sandwiches for the class picnic. Her classmates used $\frac{2}{3}$ of the bread. How many loaves of bread were used?

MODEL

• Shade the model to show $\frac{2}{3}$ of 4.

Think: I can cut the loaves into thirds and show $\frac{2}{3}$ of them being used.

 Rearrange the shaded pieces to fill as many wholes as possible.



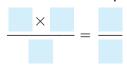
So, _____loaves of bread were used.

RECORD

 Write an expression to represent the problem.

 $\frac{2}{3} \times 4$ Think: I need to find $\frac{2}{3}$ of 4 wholes.

 Multiply 4 by the number of thirdsize pieces in each whole. Then, write the answer as the total number of third-size pieces.



• Write the answer as a mixed number.



• Would we have the same amount of bread if we had 4 groups of $\frac{2}{3}$ of a loaf? Explain.

Try This! Find the product.





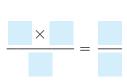
Share and Show



Find the product.

1.
$$3 \times \frac{2}{5} =$$

- Multiply the numerator by the whole number. Write the product over the denominator.
- Write the answer as a mixed number.





$$\checkmark$$
 2. $\frac{2}{3} \times 5 =$ _____

② 2.
$$\frac{2}{3} \times 5 =$$

4.
$$\frac{5}{16} \times 4 =$$

On Your Own

Find the product.

5.
$$\frac{3}{5} \times 11$$

6.
$$3 \times \frac{3}{4}$$

7.
$$\frac{5}{8} \times 3$$

MTR Find the unknown digit.

8.
$$\frac{1}{2} \times 8 = 4$$

9.
$$\times \frac{5}{6} = \frac{20}{6}$$
, or $3\frac{2}{6}$

10.
$$\frac{1}{1} \times 18 = 3$$

11. Patty wants to run $\frac{5}{6}$ of a mile every day for 5 days. Keilah wants to run $\frac{3}{4}$ of a mile every day for 6 days. Who will run the greater distance?



12. A baker made 5 pounds of dough. He used $\frac{5}{12}$ of the dough to make sandwich rolls. How much of the dough is left over?

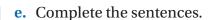
Problem Solving · Applications World

13. A chef wants to have enough turkey to feed 24 people. If he wants to provide $\frac{3}{4}$ of a pound of turkey for each person, how much turkey does he need?

a.	What do you need to find?	
	j j	



- c. What information are you given?
- **d.** Solve the problem.



The chef wants to serve 24 people

of a pound of turkey each.

He will need $___$ × $___$, or

pounds of turkey.

14. Kali is using this recipe to make salad dressing. The recipe makes 1 batch of dressing. She plans to make 5 batches of the dressing. She has 4 cups of vegetable oil. Write a multiplication expression to show how much

Does Kali have enough vegetable oil for 5 batches of the salad dressing? Explain your reasoning.

Salad Dressing

- $1\frac{1}{2}$ teaspoons paprika
- teaspoon dry mustard
- teaspoons salt
- teaspoon onion powder
- cup vegetable oil
 - cup vinegar

vegetable oil is needed for 5 batches.

Fraction and Whole Number Multiplication

Go Online

Interactive Examples

Find the product.

1.
$$4 \times \frac{5}{8} = \frac{2\frac{4}{8}}{4 \times \frac{5}{8} = \frac{20}{8}}$$
2. $\frac{17}{100} \times 3 = \frac{20}{8}$

$$\frac{20}{8} = 2\frac{4}{8}$$

2.
$$\frac{17}{100} \times 3 =$$

3.
$$\frac{4}{5} \times 10 =$$

4.
$$\frac{3}{4} \times 9 =$$

5.
$$8 \times \frac{5}{6} =$$

6.
$$7 \times \frac{1}{2} =$$

7.
$$\frac{2}{5} \times 6 =$$

8.
$$9 \times \frac{2}{3} =$$

9.
$$\frac{3}{10} \times 9 =$$

Problem Solving Real

- **10.** Linh makes aprons to sell at a craft fair. She needs $\frac{3}{4}$ yard of material to make each apron. How much material does Linh need to make 6 aprons?
- 11. The gas tank of Mr. Tanaka's car holds 15 gallons of gas. He used $\frac{2}{3}$ of a tank of gas last week. How many gallons of gas did Mr. Tanaka use?

12. WRITE Math Write a word problem that can be solved by multiplying a whole number and a fraction. Include the solution.

Lesson Check

- **13.** At the movies, Liz eats $\frac{1}{4}$ of a box of popcorn. Her friend Kyra eats two times as much popcorn as Liz eats. How much of a box of popcorn does Kyra eat?
- 14. It takes Vy 45 minutes to complete his science homework. It takes him $\frac{2}{3}$ as long to complete his math homework. How long does it take Vy to complete his math homework?

Spiral Review

- **15.** What is the best estimate for the quotient? $591 \div 29$
- **16.** Emely bought $\frac{3}{4}$ yard of red ribbon and $\frac{3}{4}$ yard of white ribbon to make some hair bows. Altogether, how many yards of ribbon did she buy?

- **17.** Azem jogged $3\frac{2}{8}$ miles on Monday, $5\frac{5}{8}$ miles on Tuesday, and 8 miles on Wednesday. Suppose he continues the pattern for the remainder of the week. How far will Azem jog on Friday?
- **18.** Qiyana bought 25 pounds of ground beef and made 100 hamburger patties of equal weight. What is the weight of each hamburger patty?

Chapter Review

answer.

1. Write $\frac{7}{16}$ as the product of a whole number and a unit fraction.

2. Marta is making 3 servings of fruit salad. She adds $\frac{3}{8}$ cup blueberries for each serving. Her measuring cup holds $\frac{1}{8}$ cup. How many times must Marta measure $\frac{1}{8}$ cup of blueberries to have enough for the fruit salad? Shade the models to show your

1/8	1/8	<u>1</u> 8	<u>1</u> 8	<u>1</u> 8	1/8	<u>1</u> 8	<u>1</u> 8
<u>1</u> 8	1/8	<u>1</u> 8	<u>1</u> 8	<u>1</u> 8	1/8	<u>1</u> 8	<u>1</u> 8
<u>1</u> 8	1/8	<u>1</u> 8	<u>1</u> 8				

Marta must measure $\frac{1}{8}$ cup _____ times.

3. Mickey watched $\frac{3}{12}$ of a 3 hour documentary. How many hours of the documentary did he watch? Complete the model to show how you found your answer?

1		1			1						
<u>1</u>	<u>1</u>	1/4	<u>1</u>								

$$\frac{3}{12} \times 3 =$$
 hour

4. Huyen is baking for the Moms and Muffins event at her school. She will bake 4 batches of banana muffins. She needs $\frac{3}{4}$ cup of bananas for each batch of muffins.

Part A

Huyen completed the multiplication below and said she needed $\frac{3}{16}$ cup of bananas for 4 batches of muffins. What is Huyen's error?

$$4 \times \frac{3}{4} = \frac{3}{16}$$

Part B

What is the correct number of cups Huyen needs for 4 batches of muffins? Explain how you found your answer.

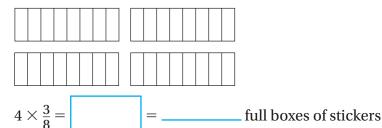
- **5.** Which fraction is a multiple of $\frac{1}{10}$? Mark all that apply.
 - $\frac{3}{10}$

- $\frac{4}{10}$

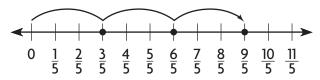
- **6.** Mimi recorded a soccer game that lasted $\frac{2}{3}$ hour. She watched it 4 times over the weekend to study the plays. How many hours did Mimi spend watching the soccer game? Show your work.

Houghton Mifflin Harcourt Publishing Company

7. Mrs. Serna is organizing her craft supplies. There are 4 open boxes of stickers in her cabinet. Each box has $\frac{3}{8}$ of the stickers remaining. How many boxes of stickers are left? Shade the model and complete the calculations below to show how you found your answer.



8. Joel made a number line showing the multiples of $\frac{3}{5}$.



The product $2 \times \frac{3}{5}$ is shown by the fraction on the number line.

9. Florian has baseball practice Monday, Wednesday, and Friday. Each practice is $\frac{5}{6}$ hour. Florian says he will have practice for 4 hours this week.

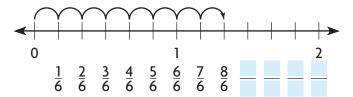
Part A

Without multiplying, explain how you know Florian is incorrect.

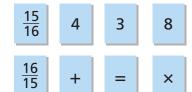
Part B

How long will Florian have baseball practice this week? Write your answer as a mixed number. Show your work.

10. Use the number line to write 4 more multiples of $\frac{1}{6}$.

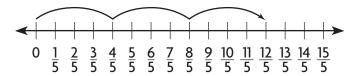


11. Imani's toy dachshund weighed $\frac{15}{16}$ pound when it was born. By age 4, the dog weighed 8 times as much. Fill each box with a number or symbol from the list to show how to find the weight of Imani's dog at age 4. Not all numbers and symbols may be used.





12. Asta made a fraction number line to help her find $3 \times \frac{4}{5}$.



Select a way to write $3 \times \frac{4}{5}$ as the product of a whole number and a unit fraction.

$$3 \times \frac{4}{5} =$$

$$4 \times \frac{3}{5}$$

$$12 \times \frac{1}{5}$$

$$6 \times \frac{1}{5}$$

13. Yusif wants to give $\frac{2}{5}$ of his total toy car collection to each of 2 of his friends. How much of his total toy car collection will he give away? Draw a model to solve the problem.

14. Select the correct product for the equation.

<u>8</u> 16

<u>32</u> 8 <u>16</u> 8

<u>20</u> 8

$$4 \times \frac{5}{8} =$$

$$4 \times \frac{4}{8} =$$

15. The lengths of different types of snakes at a zoo nursery are shown in the table.

For Problems 15a–15c, select True or False for the statement.

15a. Bobby is 4 times as long as Kenny.

True

False

15b. Bobby is 3 times

as long as Kenny.

True

False

15c. Puck is 5 times

as long as Kenny.

treat bags

True

False

Snake's NameType of SnakeLengthKennyKenyan sand boa $\frac{5}{6}$ footBobbyball python $2\frac{3}{6}$ feetPuckblood python $4\frac{1}{6}$ feet

16. Nicholas and his three friends went to the school carnival. Each of their treat bags was $\frac{6}{8}$ full. How many bags of treats did they have in total?

17. Marisha played a computer quiz game that had 20 multiple-choice questions and 10 True/False questions. She got $\frac{9}{10}$ of the multiple-choice questions correct, and she got $\frac{4}{5}$ of the True/False questions correct.

a. How many multiple-choice questions did Marisha get correct?

_____ multiple-choice questions

b. How many True/False questions did Marisha get correct?

_____True/False questions

18. Larissa bought 18 donuts. Four-sixths of the donuts have sprinkles.

Part A

How many of the donuts have sprinkles? Draw a model to show how you found your answer.



Part B

What equation can you write to represent the problem? Explain.



19. Donna buys some fabric to make placemats. She needs $\frac{1}{5}$ yard of each type of fabric. She has 9 different types of fabrics to make her design. Use the following equation. Write the number to make the statement true.

$$\frac{9}{5} = \underline{\qquad} \times \frac{1}{5}$$

20. Mr. Tuyen uses $\frac{5}{8}$ of a tank of gas each week to drive to and from his job. How many tanks of gas does Mr. Tuyen use in 5 weeks? Write your answer two different ways.

Mr. Tuyen uses _____ or ____ tanks of gas.

21. Rico is making 4 batches of salsa. Each batch needs $\frac{2}{3}$ cup of corn. He only has a $\frac{1}{3}$ -cup measure. How many times must Rico measure $\frac{1}{3}$ cup of corn to have enough for all of the salsa?

times